

M. Tech I Year I Semester Regular Examinations, February 2018  
**ADVANCED FINITE ELEMENT MENTHODS**  
**(CAD/CAM)**

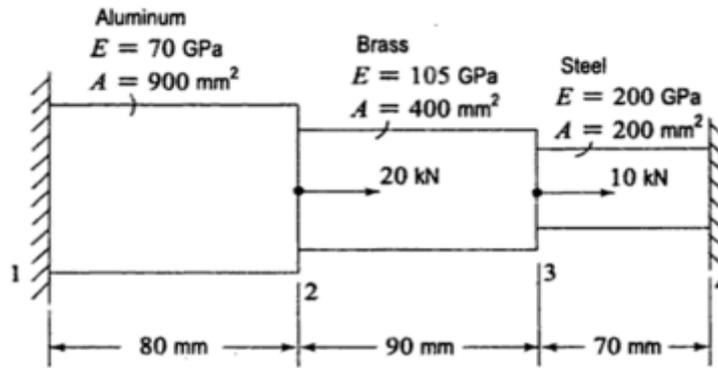
Time: 3 hours

Max Marks: 60

Answer all **five** units. (5 x 12 = 60 Marks)

**UNIT-I**

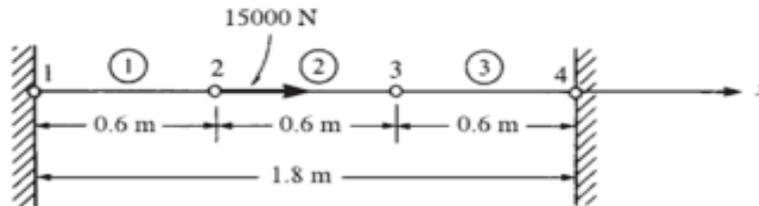
- (a) What is Finite Element Analysis (FEA)? What areas can FEA are applied?  
 (b) Mention the various coordinates in FEM. Explain any one.
- OR
- For the three-stepped bar shown in the figure, determine the displacements at nodes 2 and 3, stresses in the three sections and reactions at the ends.



**UNIT-II**

- For the three-bar assemblage shown in the figure, determine
  - Global stiffness matrix
  - Displacements at nodes 2 and 3
  - Reactions at nodes 1 and 4

A force of 15000 N is applied in the x direction at node 2. The length of each element is 0.6 m. Let  $E = 2 * 10^{11}$  Pa and  $A = 6 * 10^{-4}$  m<sup>2</sup> for elements 1 and 2, and let  $E = 1 * 10^{11}$  Pa and  $A = 12 * 10^{-4}$  m<sup>2</sup> for element 3.  
 Nodes 1 and 4 are fixed.



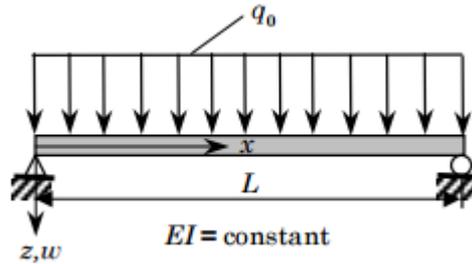
OR

- The bending moment (M) and transverse deflection (w) in a beam according to the Euler—Bernoulli beam theory are related by

$$-EI \frac{d^2w}{dx^2} = M(x)$$

For statically determinate beams, one can readily obtain the expression for the bending moment in terms of the applied loads. Thus, M(x) is a known function of x. Determine the maximum deflection of the simply supported beam under uniform load using the finite element method.

Continued in page 2



UNIT-III

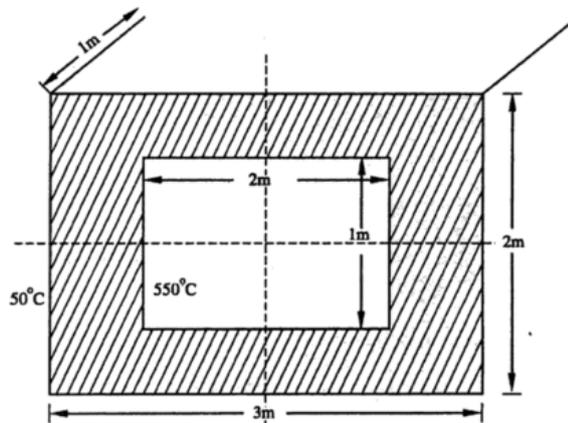
5. (a) Derive the stress – strain relationship to plane problems.  
 (b) Compare Superparametric and isoparametric representations of triangular element.

OR

6. (a) Sketch and explain the Axisymmetric solid “ring” element.  
 (b) Write a note on the Strain-Displacement Matrix.

UNIT-IV

7. (a) A furnace wall is made of fireclay brick ( $k = 1.04 \text{ W/mK}$ ). In steady state the inside and outside surfaces of the wall are at  $550^\circ \text{C}$  and  $50^\circ \text{C}$ , respectively. A schematic of the furnace wall is shown in the figure. Determine the conduction shape factor and the rate of heat conduction per metre length of the furnace.



- (b) A horizontal pipe of 10 cm radius and 5 m length is buried in a masonry brick work at a depth of 30 cm. if the pipe wall is at  $60^\circ \text{C}$  while the earth's surface is at  $5^\circ \text{C}$ , calculate the rate of heat loss by the pipe, by estimating the conduction shape factor. The thermal conductivity of masonry brick is  $0.69 \text{ W/mK}$ .

OR

8. Derive an expression for element stiffness and mass matrices for heat conduction in a thin rod.

UNIT-V

9. Explain the element consistent and lumped mass matrices for one and two dimensional linear elements.

OR

10. Find the approximate first two natural frequencies of a simply supported beam using one element.

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